

# Package ‘selectiveInference’

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**Author** Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor,  
Joshua Loftus, Stephen Reid, Jelena Markovic

**Maintainer** Rob Tibshirani <tibs@stanford.edu>

**Depends** glmnet, intervals, survival, adaptMCMC, MASS

**Suggests** Rmpfr

**Description** New tools for post-selection inference, for use with forward stepwise regression, least angle regression, the lasso, and the many means problem. The lasso function implements Gaussian, logistic and Cox survival models.

**License** GPL-2

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debiasingMatrix	<i>Find an approximate inverse of a non-negative definite matrix.</i>
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## Description

Find some rows of an approximate inverse of a non-negative definite symmetric matrix by solving optimization problem described in Javanmard and Montanari (2013). Can be used for approximate Newton step from some consistent estimator (such as the LASSO) to find a debiased solution.

## Usage

```
debiasingMatrix(Xinfo,
                is_wide,
                nsample,
                rows,
                verbose=FALSE,
                bound=NULL,
                linesearch=TRUE,
                scaling_factor=1.5,
                max_active=NULL,
                max_try=10,
                warn_kkt=FALSE,
                max_iter=50,
                kkt_stop=TRUE,
                parameter_stop=TRUE,
                objective_stop=TRUE,
                kkt_tol=1.e-4,
                parameter_tol=1.e-4,
                objective_tol=1.e-4)
```

**Arguments**

Xinfo	Either a non-negative definite matrix $S=t(X)$ is_ wide is TRUE, then Xinfo should be X, otherwise it should be S.
is_ wide	Are we solving for rows of the debiasing matrix assuming it is a wide matrix so that Xinfo=X and the non-negative definite matrix of interest is t(X)
nsample	Number of samples used in forming the cross-covariance matrix. Used for default value of the bound parameter.
rows	Which rows of the approximate inverse to compute.
verbose	Print out progress as rows are being computed.
bound	Initial bound parameter for each row. Will be changed if linesearch is TRUE.
linesearch	Run a line search to find as small as possible a bound parameter for each row?
scaling_factor	In the linesearch, the bound parameter is either multiplied or divided by this factor at each step.
max_active	How large an active set to consider in solving the problem with coordinate descent. Defaults to $\max(50, 0.3*nsample)$ .
max_try	How many tries in the linesearch.
warn_kkt	Warn if the problem does not seem to be feasible after running the coordinate descent algorithm.
max_iter	How many full iterations to run of the coordinate descent for each value of the bound parameter.
kkt_stop	If TRUE, check to stop coordinate descent when KKT conditions are approximately satisfied.
parameter_stop	If TRUE, check to stop coordinate descent based on relative convergence of parameter vector, checked at geometrically spaced iterations $2^k$ .
objective_stop	If TRUE, check to stop coordinate descent based on relative decrease of objective value, checked at geometrically spaced iterations $2^k$ .
kkt_tol	Tolerance value for assessing whether KKT conditions for solving the dual problem and feasibility of the original problem.
parameter_tol	Tolerance value for assessing convergence of the problem using relative convergence of the parameter.
objective_tol	Tolerance value for assessing convergence of the problem using relative decrease of the objective.

**Details**

This function computes an approximate inverse as described in Javanmard and Montanari (2013), specifically display (4). The problem is solved by considering a dual problem which has an objective similar to a LASSO problem and is solvable by coordinate descent. For some values of bound the original problem may not be feasible, in which case the dual problem has no solution. An attempt to detect this is made by stopping when the active set grows quite large, determined by max\_active.

**Value**

M Rows of approximate inverse of Sigma.

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**References**

Adel Javanmard and Andrea Montanari (2013). Confidence Intervals and Hypothesis Testing for High-Dimensional Regression. Arxiv: 1306.3171

**Examples**

```
set.seed(10)
n = 50
p = 100
X = matrix(rnorm(n * p), n, p)
S = t(X) %*% X / n
M = debiasingMatrix(S, FALSE, n, c(1,3,5))
M2 = debiasingMatrix(X, TRUE, n, c(1,3,5))
max(M - M2)
```

---

estimateSigma

*Estimate the noise standard deviation in regression*

---

**Description**

Estimates the standard deviation of the noise, for use in the selectiveInference package

**Usage**

```
estimateSigma(x, y, intercept=TRUE, standardize=TRUE)
```

**Arguments**

x	Matrix of predictors (n by p)
y	Vector of outcomes (length n)
intercept	Should glmnet be run with an intercept? Default is TRUE
standardize	Should glmnet be run with standardized predictors? Default is TRUE

**Details**

This function estimates the standard deviation of the noise, in a linear regression setting. A lasso regression is fit, using cross-validation to estimate the tuning parameter lambda. With sample size n, yhat equal to the predicted values and df being the number of nonzero coefficients from the lasso fit, the estimate of sigma is  $\sqrt{\text{sum}((y-\text{yhat})^2) / (n-\text{df}-1)}$ . Important: if you are using glmnet to compute the lasso estimate, be sure to use the settings for the "intercept" and "standardize" arguments in glmnet and estimateSigma. Same applies to fs or lar, where the argument for standardization is called "normalize".

**Value**

sigmahat	The estimate of sigma
df	The degrees of freedom of lasso fit used

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**References**

Stephen Reid, Jerome Friedman, and Rob Tibshirani (2014). A study of error variance estimation in lasso regression. arXiv:1311.5274.

**Examples**

```
set.seed(33)
n = 50
p = 10
sigma = 1
x = matrix(rnorm(n*p),n,p)
beta = c(3,2,rep(0,p-2))
y = x%%beta + sigma*rnorm(n)

# run forward stepwise
fsfit = fs(x,y)

# estimate sigma
sigmahat = estimateSigma(x,y)$sigmahat

# run sequential inference with estimated sigma
out = fsInf(fsfit,sigma=sigmahat)
out
```

---

factorDesign	<i>Expand a data frame with factors to form a design matrix with the full binary encoding of each factor.</i>
--------------	---

---

**Description**

When using [groupfs](#) with factor variables call this function first to create a design matrix.

**Usage**

```
factorDesign(df)
```

**Arguments**

df	Data frame containing some columns which are factors.
----	---

**Value**

List containing

**x** Design matrix, the first columns contain any numeric variables from the original date frame.

**index** Group membership indicator for expanded matrix.

**Examples**

```
## Not run:
fd = factorDesign(warpbreaks)
y = rnorm(nrow(fd$x))
fit = groupfs(fd$x, y, fd$index, maxsteps=2, intercept=F)
pvals = groupfsInf(fit)

## End(Not run)
```

---

fixedLassoInf

*Inference for the lasso, with a fixed lambda*

---

**Description**

Compute p-values and confidence intervals for the lasso estimate, at a fixed value of the tuning parameter lambda

**Usage**

```
fixedLassoInf(x,
              y,
              beta,
              lambda,
              family = c("gaussian", "binomial", "cox"),
              intercept=TRUE,
              add.targets=NULL,
              status=NULL,
              sigma=NULL,
              alpha=0.1,
              type=c("partial", "full"),
              tol.beta=1e-5,
              tol.kkt=0.1,
              gridrange=c(-100,100),
              bits=NULL,
              verbose=FALSE,
              linesearch.try=10)
```

**Arguments**

x	Matrix of predictors (n by p);
y	Vector of outcomes (length n)
beta	Estimated lasso coefficients (e.g., from glmnet). This is of length p (so the intercept is not included as the first component). Be careful! This function uses the "standard" lasso objective

$$1/2\|y - x\beta\|_2^2 + \lambda\|\beta\|_1.$$

In contrast, glmnet multiplies the first term by a factor of 1/n. So after running glmnet, to extract the beta corresponding to a value lambda, you need to use `beta = coef(obj, s=lambda/n)[-1]`, where obj is the object returned by glmnet (and [-1] removes the intercept, which glmnet always puts in the first component)

lambda	Value of lambda used to compute beta. See the above warning
family	Response type: "gaussian" (default), "binomial", or "cox" (for censored survival data)
sigma	Estimate of error standard deviation. If NULL (default), this is estimated using the mean squared residual of the full least squares fit when $n \geq 2p$ , and using the standard deviation of y when $n < 2p$ . In the latter case, the user should use <a href="#">estimateSigma</a> function for a more accurate estimate. Not used for family="binomial", or "cox"
alpha	Significance level for confidence intervals (target is miscoverage alpha/2 in each tail)
intercept	Was the lasso problem solved (e.g., by glmnet) with an intercept in the model? Default is TRUE. Must be TRUE for "binomial" family. Not used for 'cox' family, where no intercept is assumed.
add.targets	Optional vector of predictors to be included as targets of inference, regardless of whether or not they are selected by the lasso. Default is NULL.
status	Censoring status for Cox model; 1=failure 0=censored
type	Contrast type for p-values and confidence intervals: default is "partial"—meaning that the contrasts tested are the partial population regression coefficients, within the active set of predictors; the alternative is "full"—meaning that the full population regression coefficients are tested. The latter does not make sense when $p > n$ .
tol.beta	Tolerance for determining if a coefficient is zero
tol.kkt	Tolerance for determining if an entry of the subgradient is zero
gridrange	Grid range for constructing confidence intervals, on the standardized scale
bits	Number of bits to be used for p-value and confidence interval calculations. Default is NULL, in which case standard floating point calculations are performed. When not NULL, multiple precision floating point calculations are performed with the specified number of bits, using the R package Rmpfr (if this package is not installed, then a warning is thrown, and standard floating point calculations are pursued). Note: standard double precision uses 53 bits so, e.g., a

choice of 200 bits uses about 4 times double precision. The confidence interval computation is sometimes numerically challenging, and the extra precision can be helpful (though computationally more costly). In particular, extra precision might be tried if the values in the output columns of `tailarea` differ noticeably from  $\alpha/2$ .

`verbose` Print out progress along the way? Default is FALSE  
`linesearch.try` When running `type="full"` (i.e. debiased LASSO) how many attempts in the line search?

### Details

This function computes selective p-values and confidence intervals for the lasso, given a fixed value of the tuning parameter `lambda`. Three different response types are supported: gaussian, binomial and Cox. The confidence interval construction involves numerical search and can be fragile: if the observed statistic is too close to either end of the truncation interval (`vlo` and `vup`, see references), then one or possibly both endpoints of the interval of desired coverage cannot be computed, and default to  $\pm \text{Inf}$ . The output `tailarea` gives the achieved Gaussian tail areas for the reported intervals—these should be close to  $\alpha/2$ , and can be used for error-checking purposes.

Important!: Before running `glmnet` (or some other lasso-solver) `x` should be centered, that is `x <- scale(X,TRUE,FALSE)`. In addition, if standardization of the predictors is desired, `x` should be scaled as well: `x <- scale(x,TRUE,TRUE)`. Then when running `glmnet`, set `standardize=F`. See example below.

The `penalty.factor` facility in `glmnet`—allowing different penalties `lambda` for each predictor, is not yet implemented in `fixedLassoInf`. However you can finesse this— see the example below. One caveat- using this approach, a penalty factor of zero (forcing a predictor in) is not allowed.

Note that the coefficients and standard errors reported are unregularized. Eg for the Gaussian, they are the usual least squares estimates and standard errors for the model fit to the active set from the lasso.

### Value

<code>type</code>	Type of coefficients tested (partial or full)
<code>lambda</code>	Value of tuning parameter <code>lambda</code> used
<code>pv</code>	One-sided P-values for active variables, uses the fact we have conditioned on the sign.
<code>ci</code>	Confidence intervals
<code>tailarea</code>	Realized tail areas (lower and upper) for each confidence interval
<code>vlo</code>	Lower truncation limits for statistics
<code>vup</code>	Upper truncation limits for statistics
<code>vmat</code>	Linear contrasts that define the observed statistics
<code>y</code>	Vector of outcomes
<code>vars</code>	Variables in active set
<code>sign</code>	Signs of active coefficients
<code>alpha</code>	Desired coverage ( $\alpha/2$ in each tail)
<code>sigma</code>	Value of error standard deviation ( <code>sigma</code> ) used
<code>call</code>	The call to <code>fixedLassoInf</code>



**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**References**

Jason Lee, Dennis Sun, Yuekai Sun, and Jonathan Taylor (2013). Exact post-selection inference, with application to the lasso. arXiv:1311.6238.

Jonathan Taylor and Robert Tibshirani (2016) Post-selection inference for L1-penalized likelihood models. arXiv:1602.07358

**Examples**

```

set.seed(43)
n = 50
p = 10
sigma = 1

x = matrix(rnorm(n*p),n,p)
x = scale(x,TRUE,TRUE)

beta = c(3,2,rep(0,p-2))
y = x%%beta + sigma*rnorm(n)

# first run glmnet
gfit = glmnet(x,y,standardize=FALSE)

# extract coef for a given lambda; note the 1/n factor!
# (and we don't save the intercept term)
lambda = .8
beta = coef(gfit, x=x, y=y, s=lambda/n, exact=TRUE)[-1]

# compute fixed lambda p-values and selection intervals
out = fixedLassoInf(x,y,beta,lambda,sigma=sigma)
out

## as above, but use lar function instead to get initial
## lasso fit (should get same results)
lfit = lar(x,y,normalize=FALSE)
beta = coef(lfit, s=lambda, mode="lambda")
out2 = fixedLassoInf(x, y, beta, lambda, sigma=sigma)
out2

## mimic different penalty factors by first scaling x
set.seed(43)
n = 50
p = 10
sigma = 1

x = matrix(rnorm(n*p),n,p)
x=scale(x,TRUE,TRUE)

```

```

beta = c(3,2,rep(0,p-2))
y = x%%beta + sigma*rnorm(n)
pf=c(rep(1,7),rep(.1,3)) #define penalty factors
pf=p*pf/sum(pf) # penalty factors should be rescaled so they sum to p
xs=scale(x,FALSE,pf) #scale cols of x by penalty factors
# first run glmnet
gfit = glmnet(xs, y, standardize=FALSE)

# extract coef for a given lambda; note the 1/n factor!
# (and we don't save the intercept term)
lambda = .8
beta_hat = coef(gfit, x=xs, y=y, s=lambda/n, exact=TRUE)[-1]

# compute fixed lambda p-values and selection intervals
out = fixedLassoInf(xs,y,beta_hat,lambda,sigma=sigma)

#rescale conf points to undo the penalty factor
out$ci=t(scale(t(out$ci),FALSE,pf[out$vars]))
out

#logistic model
set.seed(43)

n = 50
p = 10
sigma = 1

x = matrix(rnorm(n*p),n,p)
x=scale(x,TRUE,TRUE)

beta = c(3,2,rep(0,p-2))
y = x%%beta + sigma*rnorm(n)
y=1*(y>mean(y))
# first run glmnet
gfit = glmnet(x,y,standardize=FALSE,family="binomial")

# extract coef for a given lambda; note the 1/n factor!
# (and here we DO include the intercept term)
lambda = .8
beta_hat = coef(gfit, x=x, y=y, s=lambda/n, exact=TRUE)

# compute fixed lambda p-values and selection intervals
out = fixedLassoInf(x,y,beta_hat,lambda,family="binomial")
out

# Cox model

set.seed(43)
n = 50
p = 10
sigma = 1

```

```

x = matrix(rnorm(n*p), n, p)
x = scale(x, TRUE, TRUE)

beta = c(3,2,rep(0,p-2))
tim = as.vector(x%%beta + sigma*rnorm(n))
tim= tim-min(tim)+1
status=sample(c(0,1),size=n,replace=TRUE)
# first run glmnet

y = Surv(tim,status)
gfit = glmnet(x, y, standardize=FALSE, family="cox")

# extract coef for a given lambda; note the 1/n factor!

lambda = 1.5
beta_hat = as.numeric(coef(gfit, x=x, y=y, s=lambda/n, exact=TRUE))

# compute fixed lambda p-values and selection intervals
out = fixedLassoInf(x, tim, beta_hat, lambda, status=status, family="cox")
out

# Debiased lasso or "full"

n = 50
p = 100
sigma = 1

x = matrix(rnorm(n*p),n,p)
x = scale(x,TRUE,TRUE)

beta = c(3,2,rep(0,p-2))
y = x%%beta + sigma*rnorm(n)

# first run glmnet
gfit = glmnet(x, y, standardize=FALSE, intercept=FALSE)

# extract coef for a given lambda; note the 1/n factor!
# (and we don't save the intercept term)
lambda = 2.8
beta = coef(gfit, x=x, y=y, s=lambda/n, exact=TRUE)[-1]

# compute fixed lambda p-values and selection intervals
out = fixedLassoInf(x, y, beta, lambda, sigma=sigma, type='full', intercept=FALSE)
out

# When n > p and "full" we use the full inverse
# instead of Javanmard and Montanari's approximate inverse

n = 200
p = 50
sigma = 1

```

```

x = matrix(rnorm(n*p),n,p)
x = scale(x,TRUE,TRUE)

beta = c(3,2,rep(0,p-2))
y = x%%beta + sigma*rnorm(n)

# first run glmnet
gfit = glmnet(x, y, standardize=FALSE, intercept=FALSE)

# extract coef for a given lambda; note the 1/n factor!
# (and we don't save the intercept term)
lambda = 2.8
beta = coef(gfit, x=x, y=y, s=lambda/n, exact=TRUE)[-1]

# compute fixed lambda p-values and selection intervals
out = fixedLassoInf(x, y, beta, lambda, sigma=sigma, type='full', intercept=FALSE)
out

```

---

forwardStop

*ForwardStop rule for sequential p-values*


---

### Description

Computes the ForwardStop sequential stopping rule of G'Sell et al (2014)

### Usage

```
forwardStop(pv, alpha=0.1)
```

### Arguments

pv	Vector of <b>sequential</b> p-values, for example from fsInf or larInf
alpha	Desired type FDR level (between 0 and 1)

### Details

Computes the ForwardStop sequential stopping rule of G'Sell et al (2014). Guarantees FDR control at the level alpha, for independent p-values.

### Value

Step number for sequential stop.

### Author(s)

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

## References

Max Grazier G'Sell, Stefan Wager, Alexandra Chouldechova, and Rob Tibshirani (2014). Sequential selection procedures and False Discovery Rate Control. arXiv:1309.5352. To appear in Journal of the Royal Statistical Society: Series B.

## Examples

```
set.seed(33)
n = 50
p = 10
sigma = 1
x = matrix(rnorm(n*p),n,p)
beta = c(3,2,rep(0,p-2))
y = x%%beta + sigma*rnorm(n)

# run forward stepwise
fsfit = fs(x,y)

# compute sequential p-values and confidence intervals
# (sigma estimated from full model)
out = fsInf(fsfit)
out

# estimate optimal stopping point
forwardStop(out$pv, alpha=.10)
```

---

fs	<i>Forward stepwise regression</i>
----	------------------------------------

---

## Description

This function implements forward stepwise regression, for use in the selectiveInference package

## Usage

```
fs(x, y, maxsteps=2000, intercept=TRUE, normalize=TRUE, verbose=FALSE)
```

## Arguments

x	Matrix of predictors (n by p)
y	Vector of outcomes (length n)
maxsteps	Maximum number of steps to take
intercept	Should an intercept be included on the model? Default is TRUE
normalize	Should the predictors be normalized? Default is TRUE. (Note: this argument has no real effect on model selection since forward stepwise is scale invariant already; however, it is included for completeness, and to match the interface for the <code>lar</code> function)
verbose	Print out progress along the way? Default is FALSE

**Details**

This function implements forward stepwise regression, adding the predictor at each step that maximizes the absolute correlation between the predictors—once orthogonalized with respect to the current model—and the residual. This entry criterion is standard, and is equivalent to choosing the variable that achieves the biggest drop in RSS at each step; it is used, e.g., by the `step` function in R. Note that, for example, the `lars` package implements a stepwise option (with `type="step"`), but uses a (mildly) different entry criterion, based on maximal absolute correlation between the original (non-orthogonalized) predictors and the residual.

**Value**

<code>action</code>	Vector of predictors in order of entry
<code>sign</code>	Signs of coefficients of predictors, upon entry
<code>df</code>	Degrees of freedom of each active model
<code>beta</code>	Matrix of regression coefficients for each model along the path, one column per model
<code>completepath</code>	Was the complete stepwise path computed?
<code>bls</code>	If <code>completepath</code> is TRUE, the full least squares coefficients
<code>Gamma</code>	Matrix that captures the polyhedral selection at each step
<code>nk</code>	Number of polyhedral constraints at each step in path
<code>vreg</code>	Matrix of linear contrasts that gives coefficients of variables to enter along the path
<code>x</code>	Matrix of predictors used
<code>y</code>	Vector of outcomes used
<code>bx</code>	Vector of column means of original <code>x</code>
<code>by</code>	Mean of original <code>y</code>
<code>sx</code>	Norm of each column of original <code>x</code>
<code>intercept</code>	Was an intercept included?
<code>normalize</code>	Were the predictors normalized?
<code>call</code>	The call to <code>fs</code>

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**See Also**

[fsInf](#), [predict.fs](#), [coef.fs](#), [plot.fs](#)

**Examples**

```

set.seed(33)
n = 50
p = 10
sigma = 1
x = matrix(rnorm(n*p),n,p)
beta = c(3,2,rep(0,p-2))
y = x%%beta + sigma*rnorm(n)

# run forward stepwise, plot results
fsfit = fs(x,y)
plot(fsfit)

# compute sequential p-values and confidence intervals
# (sigma estimated from full model)
out = fsInf(fsfit)
out

```

fsInf

*Selective inference for forward stepwise regression***Description**

Computes p-values and confidence intervals for forward stepwise regression

**Usage**

```

fsInf(obj, sigma=NULL, alpha=0.1, k=NULL, type=c("active","all","aic"),
      gridrange=c(-100,100), bits=NULL, mult=2, ntimes=2, verbose=FALSE)

```

**Arguments**

obj	Object returned by <code>fs</code> function
sigma	Estimate of error standard deviation. If NULL (default), this is estimated using the mean squared residual of the full least squares fit when $n \geq 2p$ , and using the standard deviation of $y$ when $n < 2p$ . In the latter case, the user should use <code>estimateSigma</code> function for a more accurate estimate
alpha	Significance level for confidence intervals (target is miscoverage $\alpha/2$ in each tail)
k	See "type" argument below. Default is NULL, in which case $k$ is taken to be the the number of steps computed in the forward stepwise path
type	Type of analysis desired: with "active" (default), p-values and confidence intervals are computed for each predictor as it is entered into the active step, all the way through $k$ steps; with "all", p-values and confidence intervals are computed for all variables in the active model after $k$ steps; with "aic", the number of steps $k$ is first estimated using a modified AIC criterion, and then the same type of analysis as in "all" is carried out for this particular value of $k$ .

Note that the AIC scheme is defined to choose a number of steps  $k$  after which the AIC criterion increases  $n$  times in a row, where  $n$  times can be specified by the user (see below). Under this definition, the AIC selection event is characterizable as a polyhedral set, and hence the extra conditioning can be taken into account exactly. Also note that an analogous BIC scheme can be specified through the `mult` argument (see below)

<code>gridrange</code>	Grid range for constructing confidence intervals, on the standardized scale
<code>bits</code>	Number of bits to be used for p-value and confidence interval calculations. Default is NULL, in which case standard floating point calculations are performed. When not NULL, multiple precision floating point calculations are performed with the specified number of bits, using the R package <code>Rmpfr</code> (if this package is not installed, then a warning is thrown, and standard floating point calculations are pursued). Note: standard double precision uses 53 bits so, e.g., a choice of 200 bits uses about 4 times double precision. The confidence interval computation is sometimes numerically challenging, and the extra precision can be helpful (though computationally more costly). In particular, extra precision might be tried if the values in the output columns of <code>tailarea</code> differ noticeably from $\alpha/2$ .
<code>mult</code>	Multiplier for the AIC-style penalty. Hence a value of 2 (default) gives AIC, whereas a value of $\log(n)$ would give BIC
<code>ntimes</code>	Number of steps for which AIC-style criterion has to increase before minimizing point is declared
<code>verbose</code>	Print out progress along the way? Default is FALSE

### Details

This function computes selective p-values and confidence intervals (selection intervals) for forward stepwise regression. The default is to report the results for each predictor after its entry into the model. See the "type" argument for other options. The confidence interval construction involves numerical search and can be fragile: if the observed statistic is too close to either end of the truncation interval (`vlo` and `vup`, see references), then one or possibly both endpoints of the interval of desired coverage cannot be computed, and default to  $\pm \text{Inf}$ . The output `tailarea` gives the achieved Gaussian tail areas for the reported intervals—these should be close to  $\alpha/2$ , and can be used for error-checking purposes.

### Value

<code>type</code>	Type of analysis (active, all, or aic)
<code>k</code>	Value of $k$ specified in call
<code>khat</code>	When type is "active", this is an estimated stopping point declared by <code>forwardStop</code> ; when type is "aic", this is the value chosen by the modified AIC scheme
<code>pv</code>	One sided P-values for active variables, uses the sign that a variable entered the model with.
<code>ci</code>	Confidence intervals
<code>tailarea</code>	Realized tail areas (lower and upper) for each confidence interval
<code>vlo</code>	Lower truncation limits for statistics



vup	Upper truncation limits for statistics
vmat	Linear contrasts that define the observed statistics
y	Vector of outcomes
vars	Variables in active set
sign	Signs of active coefficients
alpha	Desired coverage (alpha/2 in each tail)
sigma	Value of error standard deviation (sigma) used
call	The call to fsInf

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**References**

Ryan Tibshirani, Jonathan Taylor, Richard Lockhart, and Rob Tibshirani (2014). Exact post-selection inference for sequential regression procedures. arXiv:1401.3889.

Joshua Loftus and Jonathan Taylor (2014). A significance test for forward stepwise model selection. arXiv:1405.3920.

**See Also**

[fs](#)

**Examples**

```
set.seed(33)
n = 50
p = 10
sigma = 1
x = matrix(rnorm(n*p),n,p)
beta = c(3,2,rep(0,p-2))
y = x%%beta + sigma*rnorm(n)

# run forward stepwise
fsfit = fs(x,y)

# compute sequential p-values and confidence intervals
# (sigma estimated from full model)
out.seq = fsInf(fsfit)
out.seq

# compute p-values and confidence intervals after AIC stopping
out.aic = fsInf(fsfit,type="aic")
out.aic

# compute p-values and confidence intervals after 5 fixed steps
out.fix = fsInf(fsfit,type="all",k=5)
out.fix
```

---

groupfs

*Select a model with forward stepwise.*


---

## Description

This function implements forward selection of linear models almost identically to [step](#) with `direction = "forward"`. The reason this is a separate function from [fs](#) is that groups of variables (e.g. dummies encoding levels of a categorical variable) must be handled differently in the selective inference framework.

## Usage

```
groupfs(x, y, index, maxsteps, sigma = NULL, k = 2, intercept = TRUE,
        center = TRUE, normalize = TRUE, aicstop = 0, verbose = FALSE)
```

## Arguments

<code>x</code>	Matrix of predictors (n by p).
<code>y</code>	Vector of outcomes (length n).
<code>index</code>	Group membership indicator of length p. Check that <code>sort(unique(index)) = 1:G</code> where G is the number of distinct groups.
<code>maxsteps</code>	Maximum number of steps for forward stepwise.
<code>sigma</code>	Estimate of error standard deviation for use in AIC criterion. This determines the relative scale between RSS and the degrees of freedom penalty. Default is NULL corresponding to unknown sigma. When NULL, <code>link{groupfsInf}</code> performs truncated F inference instead of truncated $\chi$ . See <a href="#">extractAIC</a> for details on the AIC criterion.
<code>k</code>	Multiplier of model size penalty, the default is <code>k = 2</code> for AIC. Use <code>k = log(n)</code> for BIC, or <code>k = 2log(p)</code> for RIC (best for high dimensions, when $p > n$ ). If $G < p$ then RIC may be too restrictive and it would be better to use <code>log(G) &lt; k &lt; 2log(p)</code> .
<code>intercept</code>	Should an intercept be included in the model? Default is TRUE. Does not count as a step.
<code>center</code>	Should the columns of the design matrix be centered? Default is TRUE.
<code>normalize</code>	Should the design matrix be normalized? Default is TRUE.
<code>aicstop</code>	Early stopping if AIC increases. Default is 0 corresponding to no early stopping. Positive integer values specify the number of times the AIC is allowed to increase in a row, e.g. with <code>aicstop = 2</code> the algorithm will stop if the AIC criterion increases for 2 steps in a row. The default of <a href="#">step</a> corresponds to <code>aicstop = 1</code> .
<code>verbose</code>	Print out progress along the way? Default is FALSE.

**Value**

An object of class "groupfs" containing information about the sequence of models in the forward stepwise algorithm. Call the function `groupfsInf` on this object to compute selective p-values.

**See Also**

`groupfsInf`, `factorDesign`.

**Examples**

```
x = matrix(rnorm(20*40), nrow=20)
index = sort(rep(1:20, 2))
y = rnorm(20) + 2 * x[,1] - x[,4]
fit = groupfs(x, y, index, maxsteps = 5)
out = groupfsInf(fit)
out
```

---

`groupfsInf`

*Compute selective p-values for a model fitted by groupfs.*

---

**Description**

Computes p-values for each group of variables in a model fitted by `groupfs`. These p-values adjust for selection by truncating the usual  $\chi^2$  statistics to the regions implied by the model selection event. If the `sigma` to `groupfs` was NULL then `groupfsInf` uses truncated  $F$  statistics instead of truncated  $\chi$ . The `sigma` argument to `groupfsInf` allows users to override and use  $\chi$ , but this is not recommended unless  $\sigma$  can be estimated well (i.e.  $n > p$ ).

**Usage**

```
groupfsInf(obj, sigma = NULL, verbose = TRUE)
```

**Arguments**

<code>obj</code>	Object returned by <code>groupfs</code> function
<code>sigma</code>	Estimate of error standard deviation. Default is NULL and in this case <code>groupfsInf</code> uses the value of <code>sigma</code> specified to <code>groupfs</code> .
<code>verbose</code>	Print out progress along the way? Default is TRUE.

**Value**

An object of class "groupfsInf" containing selective p-values for the fitted model `obj`. For comparison with `fsInf`, note that the option `type = "active"` is not available.

**vars** Labels of the active groups in the order they were included.

**pv** Selective p-values computed from appropriate truncated distributions.

**sigma** Estimate of error variance used in computing p-values.

**TC or TF** Observed value of truncated  $\chi$  or  $F$ .

**df** Rank of group of variables when it was added to the model.

**support** List of intervals defining the truncation region of the corresponding statistic.

lar

*Least angle regression*

### Description

This function implements least angle regression, for use in the selectiveInference package

### Usage

```
lar(x, y, maxsteps=2000, minlam=0, intercept=TRUE, normalize=TRUE,
    verbose=FALSE)
```

### Arguments

x	Matrix of predictors (n by p)
y	Vector of outcomes (length n)
maxsteps	Maximum number of steps to take
minlam	Minimum value of lambda to consider
intercept	Should an intercept be included on the model? Default is TRUE
normalize	Should the predictors be normalized? Default is TRUE
verbose	Print out progress along the way? Default is FALSE

### Details

The least angle regression algorithm is described in detail by Efron et al. (2002). This function should match (in terms of its output) that from the lars package, but returns additional information (namely, the polyhedral constraints) needed for the selective inference calculations.

### Value

lambda	Values of lambda (knots) visited along the path
action	Vector of predictors in order of entry
sign	Signs of coefficients of predictors, upon entry
df	Degrees of freedom of each active model
beta	Matrix of regression coefficients for each model along the path, one model per column
completepath	Was the complete stepwise path computed?
bls	If completepath is TRUE, the full least squares coefficients
Gamma	Matrix that captures the polyhedral selection at each step

nk	Number of polyhedral constraints at each step in path
vreg	Matrix of linear contrasts that gives coefficients of variables to enter along the path
mp	Value of M+ (for internal use with the spacing test)
x	Matrix of predictors used
y	Vector of outcomes used
bx	Vector of column means of original x
by	Mean of original y
sx	Norm of each column of original x
intercept	Was an intercept included?
normalize	Were the predictors normalized?
call	The call to lar

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Max G'Sell, Joshua Loftus, Stephen Reid

**References**

Brad Efron, Trevor Hastie, Iain Johnstone, and Rob Tibshirani (2002). Least angle regression. *Annals of Statistics* (with discussion).

See also the descriptions in Trevor Hastie, Rob Tibshirani, and Jerome Friedman (2002, 2009). *Elements of Statistical Learning*.

**See Also**

[larInf](#), [predict.lar](#), [coef.lar](#), [plot.lar](#)

**Examples**

```
set.seed(43)
n = 50
p = 10
sigma = 1
x = matrix(rnorm(n*p),n,p)
beta = c(3,2,rep(0,p-2))
y = x%%beta + sigma*rnorm(n)

# run LAR, plot results
larfit = lar(x,y)
plot(larfit)

# compute sequential p-values and confidence intervals
# (sigma estimated from full model)
out = larInf(larfit)
out
```

---

larInf *Selective inference for least angle regression*


---

**Description**

Computes p-values and confidence intervals for least angle regression

**Usage**

```
larInf(obj, sigma=NULL, alpha=0.1, k=NULL, type=c("active","all","aic"),
       gridrange=c(-100,100), bits=NULL, mult=2, ntimes=2, verbose=FALSE)
```

**Arguments**

obj	Object returned by lar function (not the lars function!)
sigma	Estimate of error standard deviation. If NULL (default), this is estimated using the mean squared residual of the full least squares fit when $n \geq 2p$ , and using the standard deviation of $y$ when $n < 2p$ . In the latter case, the user should use <a href="#">estimateSigma</a> function for a more accurate estimate
alpha	Significance level for confidence intervals (target is miscoverage $\alpha/2$ in each tail)
k	See "type" argument below. Default is NULL, in which case $k$ is taken to be the the number of steps computed in the least angle regression path
type	Type of analysis desired: with "active" (default), p-values and confidence intervals are computed for each predictor as it is entered into the active step, all the way through $k$ steps; with "all", p-values and confidence intervals are computed for all variables in the active model after $k$ steps; with "aic", the number of steps $k$ is first estimated using a modified AIC criterion, and then the same type of analysis as in "all" is carried out for this particular value of $k$ . Note that the AIC scheme is defined to choose a number of steps $k$ after which the AIC criterion increases $ntimes$ in a row, where $ntimes$ can be specified by the user (see below). Under this definition, the AIC selection event is characterizable as a polyhedral set, and hence the extra conditioning can be taken into account exactly. Also note that an analogous BIC scheme can be specified through the <code>mult</code> argument (see below)
gridrange	Grid range for constructing confidence intervals, on the standardized scale
bits	Number of bits to be used for p-value and confidence interval calculations. Default is NULL, in which case standard floating point calculations are performed. When not NULL, multiple precision floating point calculations are performed with the specified number of bits, using the R package <code>Rmpfr</code> (if this package is not installed, then a warning is thrown, and standard floating point calculations are pursued). Note: standard double precision uses 53 bits so, e.g., a choice of 200 bits uses about 4 times double precision. The confidence interval computation is sometimes numerically challenging, and the extra precision can be helpful (though computationally more costly). In particular, extra precision

	might be tried if the values in the output columns of <code>tailarea</code> differ noticeably from $\alpha/2$ .
<code>mult</code>	Multiplier for the AIC-style penalty. Hence a value of 2 (default) gives AIC, whereas a value of $\log(n)$ would give BIC
<code>ntimes</code>	Number of steps for which AIC-style criterion has to increase before minimizing point is declared
<code>verbose</code>	Print out progress along the way? Default is FALSE

### Details

This function computes selective p-values and confidence intervals (selection intervals) for least angle regression. The default is to report the results for each predictor after its entry into the model. See the "type" argument for other options. The confidence interval construction involves numerical search and can be fragile: if the observed statistic is too close to either end of the truncation interval (`vlo` and `vup`, see references), then one or possibly both endpoints of the interval of desired coverage cannot be computed, and default to  $\pm \text{Inf}$ . The output `tailarea` gives the achieved Gaussian tail areas for the reported intervals—these should be close to  $\alpha/2$ , and can be used for error-checking purposes.

### Value

<code>type</code>	Type of analysis (active, all, or aic)
<code>k</code>	Value of k specified in call
<code>khat</code>	When type is "active", this is an estimated stopping point declared by <code>forwardStop</code> ; when type is "aic", this is the value chosen by the modified AIC scheme
<code>pv</code>	P-values for active variables
<code>ci</code>	Confidence intervals
<code>tailarea</code>	Realized tail areas (lower and upper) for each confidence interval
<code>vlo</code>	Lower truncation limits for statistics
<code>vup</code>	Upper truncation limits for statistics
<code>vmat</code>	Linear contrasts that define the observed statistics
<code>y</code>	Vector of outcomes
<code>pv.spacing</code>	P-values from the spacing test (here $M+$ is used)
<code>pv.modspac</code>	P-values from the modified form of the spacing test (here $M+$ is replaced by the next knot)
<code>pv.covtest</code>	P-values from covariance test
<code>vars</code>	Variables in active set
<code>sign</code>	Signs of active coefficients
<code>alpha</code>	Desired coverage ( $\alpha/2$ in each tail)
<code>sigma</code>	Value of error standard deviation ( $\sigma$ ) used
<code>call</code>	The call to <code>larInf</code>

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**References**

Ryan Tibshirani, Jonathan Taylor, Richard Lockhart, and Rob Tibshirani (2014). Exact post-selection inference for sequential regression procedures. arXiv:1401.3889.

**See Also**

[lar](#)

**Examples**

```
set.seed(43)
n = 50
p = 10
sigma = 1
x = matrix(rnorm(n*p),n,p)
beta = c(3,2,rep(0,p-2))
y = x%%beta + sigma*rnorm(n)

# run LAR
larfit = lar(x,y)

# compute sequential p-values and confidence intervals
# (sigma estimated from full model)
out.seq = larInf(larfit)
out.seq

# compute p-values and confidence intervals after AIC stopping
out.aic = larInf(larfit,type="aic")
out.aic

# compute p-values and confidence intervals after 5 fixed steps
out.fix = larInf(larfit,type="all",k=5)
out.fix
```

---

manyMeans

*Selective inference for many normal means*

---

**Description**

Computes p-values and confidence intervals for the largest k among many normal means

**Usage**

```
manyMeans(y, alpha=0.1, bh.q=NULL, k=NULL, sigma=1, verbose=FALSE)
```



**Arguments**

y	Vector of outcomes (length n)
alpha	Significance level for confidence intervals (target is miscoverage $\alpha/2$ in each tail)
bh.q	q parameter for BH(q) procedure
k	Number of means to consider
sigma	Estimate of error standard deviation
verbose	Print out progress along the way? Default is FALSE

**Details**

This function compute p-values and confidence intervals for the largest k among many normal means. One can specify a fixed number of means k to consider, or choose the number to consider via the BH rule.

**Value**

mu.hat	Vector of length n containing the estimated signal sizes. If a sample element is not selected, then its signal size estimate is 0
selected.set	Indices of the vector y of the sample elements that were selected by the procedure (either BH(q) or top-K). Labelled "Selind" in output table.
pv	P-values for selected signals
ci	Confidence intervals
method	Method used to choose number of means
sigma	Value of error standard deviation (sigma) used
bh.q	BH q-value used
k	Desired number of means
threshold	Computed cutoff
call	The call to manyMeans

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**References**

Stephen Reid, Jonathan Taylor, and Rob Tibshirani (2014). Post-selection point and interval estimation of signal sizes in Gaussian samples. arXiv:1405.3340.

**Examples**

```
set.seed(12345)
n = 100
mu = c(rep(3, floor(n/5)), rep(0, n-floor(n/5)))
y = mu + rnorm(n)
out = manyMeans(y, bh.q=0.1)
out
```

---

`plot.fs`*Plot function for forward stepwise regression*

---

**Description**

Plot coefficient profiles along the forward stepwise path

**Usage**

```
## S3 method for class 'fs'  
plot(x, breaks=TRUE, omit.zeros=TRUE, var.labels=TRUE, ...)
```

**Arguments**

<code>x</code>	Object returned by a call to <code>fs</code> function
<code>breaks</code>	Should vertical lines be drawn at each break point in the piecewise linear coefficient paths? Default is TRUE
<code>omit.zeros</code>	Should segments of the coefficients paths that are equal to zero be omitted (to avoid clutter in the figure)? Default is TRUE
<code>var.labels</code>	Should paths be labelled with corresponding variable numbers? Default is TRUE
<code>...</code>	Additional arguments for plotting

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**Examples**

```
set.seed(33)  
n = 50  
p = 10  
sigma = 1  
x = matrix(rnorm(n*p),n,p)  
beta = c(3,2,rep(0,p-2))  
y = x%%beta + sigma*rnorm(n)  
  
# run forward stepwise, plot results  
fsfit = fs(x,y)  
plot(fsfit)
```

---

`plot.lar`*Plot function for least angle regression*

---

**Description**

Plot coefficient profiles along the LAR path

**Usage**

```
## S3 method for class 'lar'  
plot(x, xvar=c("norm","step","lambda"), breaks=TRUE,  
      omit.zeros=TRUE, var.labels=TRUE, ...)
```

**Arguments**

<code>x</code>	Object returned by a call to <code>lar</code> function (not the <code>lars</code> function!)
<code>xvar</code>	Either "norm" or "step" or "lambda", determining what is plotted on the x-axis
<code>breaks</code>	Should vertical lines be drawn at each break point in the piecewise linear coefficient paths? Default is TRUE
<code>omit.zeros</code>	Should segments of the coefficients paths that are equal to zero be omitted (to avoid clutter in the figure)? Default is TRUE
<code>var.labels</code>	Should paths be labelled with corresponding variable numbers? Default is TRUE
<code>...</code>	Additional arguments for plotting

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**Examples**

```
set.seed(43)  
n = 50  
p = 10  
sigma = 1  
x = matrix(rnorm(n*p),n,p)  
beta = c(3,2,rep(0,p-2))  
y = x%%beta + sigma*rnorm(n)  
  
# run LAR, plot results  
larfit = lar(x,y)  
plot(larfit)
```

---

`predict.fs`*Prediction and coefficient functions for forward stepwise regression*

---

**Description**

Make predictions or extract coefficients from a forward stepwise object

**Usage**

```
## S3 method for class 'fs'  
predict(object, newx, s, ...)  
## S3 method for class 'fs'  
coef(object, s, ...)
```

**Arguments**

<code>object</code>	Object returned by a call to <code>fs</code> function
<code>newx</code>	Matrix of <code>x</code> values at which the predictions are desired. If <code>NULL</code> , the <code>x</code> values from forward stepwise fitting are used
<code>s</code>	Step number(s) at which predictions or coefficients are desired
<code>...</code>	Additional arguments

**Value**

Either a vector/matrix of predictions, or a vector/matrix of coefficients.

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**Examples**

```
set.seed(33)  
n = 200  
p = 20  
sigma = 1  
x = matrix(rnorm(n*p),n,p)  
beta = c(rep(3,10),rep(0,p-10))  
y = x*%beta + sigma*rnorm(n)  
  
# run forward stepwise and predict functions  
obj = fs(x,y)  
fit = predict(obj,x,s=3)
```

---

predict.groupfs      *Prediction and coefficient functions for groupfs.*

---

**Description**

Make predictions or extract coefficients from a groupfs forward stepwise object.

**Usage**

```
## S3 method for class 'groupfs'
predict(object, newx)
```

**Arguments**

object	Object returned by a call to <code>groupfs</code> .
newx	Matrix of x values at which the predictions are desired. If NULL, the x values from groupfs fitting are used.

**Value**

A vector of predictions or a vector of coefficients.

---

predict.lar      *Prediction and coefficient functions for least angle regression*

---

**Description**

Make predictions or extract coefficients from a least angle regression object

**Usage**

```
## S3 method for class 'lar'
predict(object, newx, s, mode=c("step","lambda"), ...)
## S3 method for class 'lar'
coef(object, s, mode=c("step","lambda"), ...)
```

**Arguments**

object	Object returned by a call to lar function (not the lars function!)
newx	Matrix of x values at which the predictions are desired. If NULL, the x values from least angle regression fitting are used
s	Step number(s) or lambda value(s) at which predictions or coefficients are desired
mode	Either "step" or "lambda", determining the role of s (above)
...	Additional arguments

**Value**

Either a vector/matrix of predictions, or a vector/matrix of coefficients.

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**Examples**

```
set.seed(33)
n = 200
p = 20
sigma = 1
x = matrix(rnorm(n*p),n,p)
beta = c(rep(3,10),rep(0,p-10))
y = x%%beta + sigma*rnorm(n)

# run lar and predict functions
obj = lar(x,y)
fit = predict(obj,x,s=3)
```

---

randomizedLasso

*Inference for the randomized lasso, with a fixed lambda*

---

**Description**

Solve a randomly perturbed LASSO problem.

**Usage**

```
randomizedLasso(X,
                y,
                lam,
                family=c("gaussian", "binomial"),
                noise_scale=NULL,
                ridge_term=NULL,
                max_iter=100,
                kkt_tol=1.e-4,
                parameter_tol=1.e-8,
                objective_tol=1.e-8,
                objective_stop=FALSE,
                kkt_stop=TRUE,
                parameter_stop=TRUE)
```

**Arguments**

x	Matrix of predictors (n by p);
y	Vector of outcomes (length n)
lam	Value of lambda used to compute beta. See the above warning Be careful! This function uses the "standard" lasso objective

$$1/2\|y - x\beta\|_2^2 + \lambda\|\beta\|_1.$$

In contrast, glmnet multiplies the first term by a factor of 1/n. So after running glmnet, to extract the beta corresponding to a value lambda, you need to use `beta = coef(obj, s=lambda/n)[-1]`, where obj is the object returned by glmnet (and [-1] removes the intercept, which glmnet always puts in the first component)

family	Response type: "gaussian" (default), "binomial".
noise_scale	Scale of Gaussian noise added to objective. Default is 0.5 * sd(y) times the sqrt of the mean of the trace of X^TX.
ridge_term	A small "elastic net" or ridge penalty is added to ensure the randomized problem has a solution. 0.5 * sd(y) times the sqrt of the mean of the trace of X^TX divided by sqrt(n).
max_iter	How many rounds of updates used of coordinate descent in solving randomized LASSO.
kkt_tol	Tolerance for checking convergence based on KKT conditions.
parameter_tol	Tolerance for checking convergence based on convergence of parameters.
objective_tol	Tolerance for checking convergence based on convergence of objective value.
kkt_stop	Should we use KKT check to determine when to stop?
parameter_stop	Should we use convergence of parameters to determine when to stop?
objective_stop	Should we use convergence of objective value to determine when to stop?

**Details**

For family="gaussian" this function uses the "standard" lasso objective

$$1/2\|y - x\beta\|_2^2 + \lambda\|\beta\|_1$$

and adds a term

$$-\omega^T\beta + \frac{\epsilon}{2}\|\beta\|_2^2$$

where omega is drawn from IID normals with standard deviation noise\_scale and epsilon given by ridge\_term. See below for default values of noise\_scale and ridge\_term.

For family="binomial", the squared error loss is replaced by the negative of the logistic log-likelihood.

**Value**

X	Design matrix.
y	Response vector.
lam	Vector of penalty parameters.
family	Family: "gaussian" or "binomial".
active_set	Set of non-zero coefficients in randomized solution that were penalized. Integers from 1:p.
inactive_set	Set of zero coefficients in randomized solution. Integers from 1:p.
unpenalized_set	Set of non-zero coefficients in randomized solution that were not penalized. Integers from 1:p.
sign_soln	The sign pattern of the randomized solution.
full_law	List describing sampling parameters for conditional law of all optimization variables given the data in the LASSO problem.
conditional_law	List describing sampling parameters for conditional law of only the scaling variables given the data and the observed subgradient in the LASSO problem.
internal_transform	Affine transformation describing relationship between internal representation of the data and the data component of score of the likelihood at the unregularized MLE based on the sign_vector (a.k.a. relaxed LASSO).
observed_raw	Data component of the score at the unregularized MLE.
noise_scale	SD of Gaussian noise used to draw the perturbed objective.
soln	The randomized solution. Inference is made conditional on its sign vector (so no more snooping of this value is formally permitted.) If condition_subgrad == TRUE when sampling, then we may snoop on the observed subgradient.
perturb	The random vector in the linear term added to the objective.

**Author(s)**

Jelena Markovic, Jonathan Taylor

**References**

- Xiaoying Tian, and Jonathan Taylor (2015). Selective inference with a randomized response. [arxiv.org:1507.06739](https://arxiv.org/abs/1507.06739)
- Xiaoying Tian, Snigdha Panigrahi, Jelena Markovic, Nan Bi and Jonathan Taylor (2016). Selective inference after solving a convex problem. [arxiv:1609.05609](https://arxiv.org/abs/1609.05609)

**Examples**

```
set.seed(43)
n = 50
p = 10
sigma = 0.2
```



```

lam = 0.5

X = matrix(rnorm(n*p), n, p)
X = scale(X, TRUE, TRUE) / sqrt(n-1)

beta = c(3,2,rep(0,p-2))
y = X%%beta + sigma*rnorm(n)

result = randomizedLasso(X, y, lam)

```

---

randomizedLassoInf      *Inference for the randomized lasso, with a fixed lambda*

---

### Description

Compute p-values and confidence intervals based on selecting an active set with the randomized lasso, at a fixed value of the tuning parameter lambda and using Gaussian randomization.

### Usage

```

randomizedLassoInf(rand_lasso_soln,
  targets=NULL,
                    level=0.9,
                    sampler=c("norejection", "adaptMCMC"),
                    nsample=10000,
                    burnin=2000,
                    opt_samples=NULL)

```

### Arguments

**rand\_lasso\_soln**      A randomized lasso solution as returned by randomizedLasso.

**targets**              If not NULL, should be a list with entries observed\_target, cov\_target, crosscov\_target\_internal. The observed\_target should be (pre-selection) asymptotically Gaussian around targeted parameters. The quantity cov\_target should be an estimate of the (pre-selection) covariance of observed\_target. Finally, crosscov\_target\_internal should be an estimate of the (pre-selection) covariance of observed\_target and the internal representation of the data of the LASSO. For both "gaussian" and "binomial", this is the vector

$$\hat{\beta}_{E,MLE}, X_{-E}^T (y - \mu(X_E \hat{\beta}_{E,MLE}))$$

For example, this cross-covariance could be estimated by jointly bootstrapping the target of interest and the above vector.

**level**                Level for confidence intervals.

**sampler**             Which sampler to use – default is a no-rejection sampler. Otherwise use MCMC from the adaptMCMC package.

<code>nsample</code>	Number of samples of optimization variables to sample.
<code>burnin</code>	How many samples of optimization variable to discard (should be less than <code>nsample</code> ).
<code>opt_samples</code>	Optional sample of optimization variables. If not NULL then no MCMC will be run.

**Details**

This function computes selective p-values and confidence intervals for a randomized version of the lasso, given a fixed value of the tuning parameter `lambda`.

**Value**

<code>targets</code>	A list with entries <code>observed_target</code> , <code>cov_target</code> , <code>crosscov_target_internal</code> . See argument description above.
<code>pvalues</code>	P-values testing hypotheses that each specific target is 0.
<code>ci</code>	Confidence interval for parameters determined by targets.

**Author(s)**

Jelena Markovic, Jonathan Taylor

**References**

Jelena Markovic and Jonathan Taylor (2016). Bootstrap inference after using multiple queries for model selection. [arxiv.org:1612.07811](https://arxiv.org/abs/1612.07811)

Xiaoying Tian and Jonathan Taylor (2015). Selective inference with a randomized response. [arxiv.org:1507.06739](https://arxiv.org/abs/1507.06739)

Xiaoying Tian, Snigdha Panigrahi, Jelena Markovic, Nan Bi and Jonathan Taylor (2016). Selective inference after solving a convex problem. [arxiv.org:1609.05609](https://arxiv.org/abs/1609.05609)

**Examples**

```
set.seed(43)
n = 50
p = 10
sigma = 0.2
lam = 0.5

X = matrix(rnorm(n*p), n, p)
X = scale(X, TRUE, TRUE) / sqrt(n-1)

beta = c(3,2,rep(0,p-2))
y = X%%beta + sigma*rnorm(n)

result = randomizedLasso(X, y, lam)
inf_result = randomizedLassoInf(result)
```

**Description**

Compute p-values and confidence intervals for the lasso estimate, at a fixed value of the tuning parameter lambda using the "relevant" conditioning event of [arxiv.org/1801.09037](https://arxiv.org/1801.09037).

**Usage**

```
ROSI(X,
      y,
      soln,
      lambda,
      penalty_factor=NULL,
      dispersion=1,
      family=c('gaussian', 'binomial'),
      solver=c('QP', 'glmnet'),
      construct_ci=TRUE,
      debiasing_method=c("JM", "BN"),
      verbose=FALSE,
      level=0.9,
      use_debiased=TRUE)
```

**Arguments**

X	Matrix of predictors (n by p);
y	Vector of outcomes (length n)
soln	Estimated lasso coefficients (e.g., from glmnet). This is of length p (so the intercept is not included as the first component). Be careful! This function uses the "standard" lasso objective

$$1/2\|y - X\beta\|_2^2 + \lambda\|\beta\|_1.$$

In contrast, glmnet multiplies the first term by a factor of 1/n. So after running glmnet, to extract the beta corresponding to a value lambda, you need to use `beta = coef(obj, s=lambda/n)[-1]`, where obj is the object returned by glmnet (and [-1] removes the intercept, which glmnet always puts in the first component)

lambda	Value of lambda used to compute beta. See the above warning
penalty_factor	Penalty factor as used by glmnet. Actual penalty used in solving the problem is

$$\lambda \cdot \sum_{i=1}^p f_i |\beta_i|$$

with f being the penalty\_factor. Defaults to vector of 1s.

dispersion	Estimate of dispersion in the GLM. Can be taken to be 1 for logisitic and should be an estimate of the error variance for the Gaussian.
family	Family used for likelihood.
solver	Solver used to solve restricted problems needed to find truncation set. Each active variable requires solving a new LASSO problem obtained by zeroing out one coordinate of original problem. The "QP" choice uses coordinate descent for a specific value of lambda, rather than glmnet which would solve for a new path each time.
construct_ci	Report confidence intervals or just p-values?
debiasing_method	Which method should be used for debiasing? Choices are "JM" (Javanmard, Montanari) or "BN" (method described in <a href="https://arxiv.org/1703.03282">arxiv.org/1703.03282</a> ).
verbose	Print out progress along the way? Default is FALSE.
level	Confidence level for intervals.
use_debiased	Use the debiased estimate of the parameter or not. When FALSE, this is the method described in <a href="https://arxiv.org/1801.09037">arxiv.org/1801.09037</a> . The default TRUE often produces noticeably shorter intervals and more powerful tests when p is comparable to n. Ignored when $n < p$ and set to TRUE. Also note that with "BN" as debiasing method and $n > p$ , this agrees with method in <a href="https://arxiv.org/1801.09037">arxiv.org/1801.09037</a> .

## Details

???

## Value

active_set	Active set of LASSO.
pvalues	Two-sided P-values for active variables.
intervals	Confidence intervals
estimate	Relaxed (i.e. unshrunk) selected estimates.
std_err	Standard error of relaxed estimates (pre-selection).
dispersion	Dispersion parameter.
lower_trunc	Lower truncation point. The estimates should be outside the interval formed by the lower and upper truncation points.
upper_trunc	Upper truncation point. The estimates should be outside the interval formed by the lower and upper truncation points.
lambda	Value of tuning parameter lambda used.
penalty_factor	Penalty factor used for solving problem.
level	Confidence level.
call	The call to fixedLassoInf.

## Author(s)

Jelena Markovic, Jonathan Taylor

## References

Keli Liu, Jelena Markovic, Robert Tibshirani. More powerful post-selection inference, with application to the Lasso. arXiv:1801.09037

Tom Boot, Didier Nibbering. Inference in high-dimensional linear regression models. arXiv:1703.03282

## Examples

```

library(selectiveInference)
library(glmnet)
set.seed(43)

n = 100
p = 200
s = 2
sigma = 1

x = matrix(rnorm(n*p),n,p)
x = scale(x,TRUE,TRUE)

beta = c(rep(10, s), rep(0,p-s)) / sqrt(n)
y = x %*% beta + sigma*rnorm(n)

# first run glmnet
gfit = glmnet(x,y,standardize=FALSE)

# extract coef for a given lambda; note the 1/n factor!
# (and we don't save the intercept term)
lambda = 4 * sqrt(n)
lambda_glmnet = 4 / sqrt(n)
beta = selectiveInference:::solve_problem_glmnet(x,
                                                y,
                                                lambda_glmnet,
                                                penalty_factor=rep(1, p),
                                                family="gaussian")

# compute fixed lambda p-values and selection intervals
out = ROSI(x,
          y,
          beta,
          lambda,
          dispersion=sigma^2)

out

# an alternate approximate inverse from Boot and Nibbering

out = ROSI(x,
          y,
          beta,
          lambda,
          dispersion=sigma^2,
          debiasing_method="BN")

```

out

---

scaleGroups                      *Center and scale design matrix by groups*

---

### Description

For internal use by [groupfs](#).

### Usage

```
scaleGroups(x, index, center = TRUE, normalize = TRUE)
```

### Arguments

x	Design matrix.
index	Group membership indicator of length p.
center	Center groups, default is TRUE.
normalize	Scale groups by Frobenius norm, default is TRUE.

### Value

**x** Optionally centered/scaled design matrix.  
**xm** Means of groups in original design matrix.  
**xs** Frobenius norms of groups in original design matrix.

---

selectiveInference            *Tools for selective inference*

---

### Description

Functions to perform post-selection inference for forward stepwise regression, least angle regression, the lasso and the many normal means problem. The lasso function also supports logistic regression and the Cox model.

### Details

Package: selectiveInference  
 Type: Package  
 License: GPL-2

This package provides tools for inference after selection, in forward stepwise regression, least angle regression, the lasso, and the many normal means problem. The functions compute p-values and selection intervals that properly account for the inherent selection carried out by the procedure. These have exact finite sample type I error and coverage under Gaussian errors. For the logistic and Cox families (fixedLassoInf), the coverage is asymptotically valid

This R package was developed as part of the selective inference software project in Python and R:

<https://github.com/selective-inference>

Some of the R code in this work is a modification of Python code from this repository. Here is the current selective inference software team:

Yuval Benjamini, Leonard Blier, Will Fithian, Jason Lee, Joshua Loftus, Stephen Reid, Dennis Sun, Yuekai Sun, Jonathan Taylor, Xiaoying Tian, Ryan Tibshirani, Rob Tibshirani

The main functions included in the package are: `fs`, `fsInf`, `lar`, `larInf`, `fixedLassoInf`, `manyMeans`

### Author(s)

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

Maintainer: Rob Tibshirani <tibs@stanford.edu>

### References

Ryan Tibshirani, Jonathan Taylor, Richard Lockhart, and Rob Tibshirani (2014). Exact post-selection inference for sequential regression procedures. arXiv:1401.3889.

Jason Lee, Dennis Sun, Yuekai Sun, and Jonathan Taylor (2013). Exact post-selection inference, with application to the lasso. arXiv:1311.6238.

Stephen Reid, Jonathan Taylor, and Rob Tibshirani (2014). Post-selection point and interval estimation of signal sizes in Gaussian samples. arXiv:1405.3340.

Jonathan Taylor and Robert Tibshirani (2016) Post-selection inference for L1-penalized likelihood models. arXiv:1602.07358

### Examples

```
set.seed(33)
n = 50
p = 10
sigma = 1
x = matrix(rnorm(n*p),n,p)
beta = c(3,2,rep(0,p-2))
y = x%%beta + sigma*rnorm(n)

# run forward stepwise
fsfit = fs(x,y)

# compute sequential p-values and confidence intervals
# (sigma estimated from full model)
out.seq = fsInf(fsfit)
out.seq

# compute p-values and confidence intervals after AIC stopping
```

```

out.aic = fsInf(fsfit,type="aic")
out.aic

# compute p-values and confidence intervals after 5 fixed steps
out.fix = fsInf(fsfit,type="all",k=5)
out.fix

## NOT RUN---lasso at fixed lambda- Gaussian family
## first run glmnet
# gfit = glmnet(x,y)

## extract coef for a given lambda; note the 1/n factor!
## (and we don't save the intercept term)
# lambda = .1
# beta = coef(gfit, s=lambda/n, exact=TRUE)[-1]

## compute fixed lambda p-values and selection intervals
# out = fixedLassoInf(x,y,beta,lambda,sigma=sigma)
# out

#lasso at fixed lambda- logistic family
#set.seed(43)
# n = 50
# p = 10
# sigma = 1

# x = matrix(rnorm(n*p),n,p)
x=scale(x,TRUE,TRUE)
#
# beta = c(3,2,rep(0,p-2))
# y = x%%beta + sigma*rnorm(n)
# y=1*(y>mean(y))
# first run glmnet
# gfit = glmnet(x,y,standardize=FALSE,family="binomial")

# extract coef for a given lambda; note the 1/n factor!
# (and here we DO include the intercept term)
# lambda = .8
# beta = coef(gfit, s=lambda/n, exact=TRUE)

# # compute fixed lambda p-values and selection intervals
# out = fixedLassoInf(x,y,beta,lambda,family="binomial")
# out

##lasso at fixed lambda- Cox family
#set.seed(43)
# n = 50
# p = 10
# sigma = 1

# x = matrix(rnorm(n*p),n,p)
# x=scale(x,TRUE,TRUE)

```



```

# beta = c(3,2,rep(0,p-2))
# tim = as.vector(x%%beta + sigma*rnorm(n))
# tim= tim-min(tim)+1
#status=sample(c(0,1),size=n,replace=T)
# first run glmnet
# gfit = glmnet(x, Surv(tim,status),standardize=FALSE,family="cox")
# extract coef for a given lambda; note the 1/n factor!

# lambda = 1.5
# beta = as.numeric(coef(gfit, s=lambda/n, exact=TRUE))

# compute fixed lambda p-values and selection intervals
# out = fixedLassoInf(x,tim,beta,lambda,status=status,family="cox")
# out
## NOT RUN---many normal means
# set.seed(12345)
# n = 100
# mu = c(rep(3,floor(n/5)), rep(0,n-floor(n/5)))
# y = mu + rnorm(n)
# out = manyMeans(y, bh.q=0.1)
# out

## NOT RUN---forward stepwise with groups
# set.seed(1)
# n = 20
# p = 40
# x = matrix(rnorm(n*p), nrow=n)
# index = sort(rep(1:(p/2), 2))
# y = rnorm(n) + 2 * x[,1] - x[,4]
# fit = groupfs(x, y, index, maxsteps = 5)
# out = groupfsInf(fit)
# out

## NOT RUN---estimation of sigma for use in fsInf
## (or larInf or fixedLassoInf)
# set.seed(33)
# n = 50
# p = 10
# sigma = 1
# x = matrix(rnorm(n*p),n,p)
# beta = c(3,2,rep(0,p-2))
# y = x%%beta + sigma*rnorm(n)

## run forward stepwise
# fsfit = fs(x,y)

## estimate sigma
# sigmahat = estimateSigma(x,y)$sigmahat

## run sequential inference with estimated sigma
# out = fsInf(fit,sigma=sigmahat)
# out

```

---

 TG.interval

*Truncated Gaussian confidence interval.*


---

### Description

Compute truncated Gaussian interval of Lee et al. (2016) with arbitrary affine selection and covariance. Z should satisfy A

### Usage

```
TG.interval(Z, A, b, eta, Sigma=NULL, alpha=0.1,
            gridrange=c(-100,100),
                gridpts=100,
                griddepth=2,
                flip=FALSE,
                bits=NULL)
```

### Arguments

Z	Observed data (assumed to follow $N(\mu, \Sigma)$ with $\text{sum}(\eta * \mu) = \text{null\_value}$ )
A	Matrix specifying affine inequalities $AZ \leq b$
b	Offsets in the affine inequalities $AZ \leq b$ .
eta	Determines the target $\text{sum}(\eta * \mu)$ and estimate $\text{sum}(\eta * Z)$ .
Sigma	Covariance matrix of Z. Defaults to identity.
alpha	Significance level for confidence intervals (target is miscoverage $\alpha/2$ in each tail)
gridrange	Grid range for constructing confidence intervals, on the standardized scale.
gridpts	???????
griddepth	???????
flip	???????
bits	Number of bits to be used for p-value and confidence interval calculations. Default is NULL, in which case standard floating point calculations are performed. When not NULL, multiple precision floating point calculations are performed with the specified number of bits, using the R package <code>Rmpfr</code> (if this package is not installed, then a warning is thrown, and standard floating point calculations are pursued). Note: standard double precision uses 53 bits so, e.g., a choice of 200 bits uses about 4 times double precision. The confidence interval computation is sometimes numerically challenging, and the extra precision can be helpful (though computationally more costly). In particular, extra precision might be tried if the values in the output columns of <code>tailarea</code> differ noticeably from $\alpha/2$ .

**Details**

This function computes selective confidence intervals based on the polyhedral lemma of Lee et al. (2016).

**Value**

int                    Selective confidence interval.  
 tailarea              Realized tail areas (lower and upper) for each confidence interval.

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**References**

Jason Lee, Dennis Sun, Yuekai Sun, and Jonathan Taylor (2016). Exact post-selection inference, with application to the lasso. *Annals of Statistics*, 44(3), 907-927.

Jonathan Taylor and Robert Tibshirani (2017) Post-selection inference for math L1-penalized likelihood models. *Canadian Journal of Statistics*, xx, 1-21. (Volume still not posted)

**Examples**

```
A = diag(5)
b = rep(1, 5)
Z = rep(0, 5)
Sigma = diag(5)
eta = as.numeric(c(1, 1, 0, 0, 0))
TG.interval(Z, A, b, eta, Sigma)
```

---

 TG.limits

*Truncation limits and standard deviation.*


---

**Description**

Compute truncated limits and SD for use in computing p-values or confidence intervals of Lee et al. (2016). Z should satisfy A

**Usage**

```
TG.limits(Z, A, b, eta, Sigma)
```

**Arguments**

Z                    Observed data (assumed to follow  $N(\mu, \Sigma)$  with  $\text{sum}(\eta * \mu) = \text{null\_value}$ )  
 A                    Matrix specifying affine inequalities  $AZ \leq b$   
 b                    Offsets in the affine inequalities  $AZ \leq b$ .  
 eta                  Determines the target  $\text{sum}(\eta * \mu)$  and estimate  $\text{sum}(\eta * Z)$ .  
 Sigma                Covariance matrix of Z. Defaults to identity.

**Details**

This function computes the limits of truncation and the implied standard deviation in the polyhedral lemma of Lee et al. (2016).

**Value**

vlo	Lower truncation limits for statistic
vup	Upper truncation limits for statistic
sd	Standard error of $\text{sum}(\eta * Z)$

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**References**

Jason Lee, Dennis Sun, Yuekai Sun, and Jonathan Taylor (2016). Exact post-selection inference, with application to the lasso. *Annals of Statistics*, 44(3), 907-927.

Jonathan Taylor and Robert Tibshirani (2017) Post-selection inference for math L1-penalized likelihood models. *Canadian Journal of Statistics*, xx, 1-21. (Volume still not posted)

**Examples**

```
A = diag(5)
b = rep(1, 5)
Z = rep(0, 5)
Sigma = diag(5)
eta = as.numeric(c(1, 1, 0, 0, 0))
TG.limits(Z, A, b, eta, Sigma)
```

---

TG.pvalue

*Truncated Gaussian p-value.*

---

**Description**

Compute truncated Gaussian p-value of Lee et al. (2016) with arbitrary affine selection and covariance. Z should satisfy A

**Usage**

```
TG.pvalue(Z, A, b, eta, Sigma, null_value=0, bits=NULL)
```

**Arguments**

Z	Observed data (assumed to follow $N(\mu, \Sigma)$ with $\text{sum}(\eta * \mu) = \text{null\_value}$ )
A	Matrix specifying affine inequalities $AZ \leq b$
b	Offsets in the affine inequalities $AZ \leq b$ .
eta	Determines the target $\text{sum}(\eta * \mu)$ and estimate $\text{sum}(\eta * Z)$ .
Sigma	Covariance matrix of Z. Defaults to identity.
null_value	Hypothesized value of $\text{sum}(\eta * \mu)$ under the null.
bits	Number of bits to be used for p-value and confidence interval calculations. Default is NULL, in which case standard floating point calculations are performed. When not NULL, multiple precision floating point calculations are performed with the specified number of bits, using the R package <code>Rmpfr</code> (if this package is not installed, then a warning is thrown, and standard floating point calculations are pursued). Note: standard double precision uses 53 bits so, e.g., a choice of 200 bits uses about 4 times double precision. The confidence interval computation is sometimes numerically challenging, and the extra precision can be helpful (though computationally more costly). In particular, extra precision might be tried if the values in the output columns of <code>tailarea</code> differ noticeably from $\alpha/2$ .

**Details**

This function computes selective p-values based on the polyhedral lemma of Lee et al. (2016).

**Value**

pv	One-sided P-values for active variables, uses the fact we have conditioned on the sign.
vlo	Lower truncation limits for statistic
vup	Upper truncation limits for statistic
sd	Standard error of $\text{sum}(\eta * Z)$

**Author(s)**

Ryan Tibshirani, Rob Tibshirani, Jonathan Taylor, Joshua Loftus, Stephen Reid

**References**

- Jason Lee, Dennis Sun, Yuekai Sun, and Jonathan Taylor (2016). Exact post-selection inference, with application to the lasso. *Annals of Statistics*, 44(3), 907-927.
- Jonathan Taylor and Robert Tibshirani (2017) Post-selection inference for math L1-penalized likelihood models. *Canadian Journal of Statistics*, xx, 1-21. (Volume still not posted)

**Examples**

```
A = diag(5)
b = rep(1, 5)
Z = rep(0, 5)
Sigma = diag(5)
eta = as.numeric(c(1, 1, 0, 0, 0))
TG.pvalue(Z, A, b, eta, Sigma)
TG.pvalue(Z, A, b, eta, Sigma, null_value=1)
```

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